

Artículo de Investigación

FLEXURAL RIGIDITY OF THE COLOMBIAN ANDES

Rigidez de flexión de los andes colombianos

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Abstract

This work makes computes of Flexural Rigidity values, through using Moho deflection models with Bouguer gravity anomaly data and topographical heights over three profiles that pass across and covers the three Andean mountain belts of Colombia. Finally a discussion is made between the obtained results and previous works in the same study area.

Key words: Elastic thickness, satellite, flexure, Bouguer anomaly, topography.

Resumen

En este trabajo se realiza el cálculo de valores de rigidez flexural mediante el empleo de modelos de deflexión del moho con datos de anomalía de gravedad de Bouguer y alturas topográficas, en perfiles que cubren las tres cordilleras. Finalmente, se realiza una discusión entre los resultados obtenidos y estudios previos para la misma área de estudio.

Palabras clave: espesor elástico, satélite, anomalía de Bouguer, topografía.

Introduction

Several Geological phenomena allow that in long term Earth's lithosphere has an elastic behavior; in fact, Effective Elastic Thickness is a proof of that. The study of the elastic behavior of lithosphere is relevant to determine its stress condition and the analysis of distribution of these in the lithosphere helps in the research of natural phenomena and hazards as earthquakes, because occurrence of these reveals the force loads on which the lithosphere has subjected. Flexural rigidity is the resistance measure that the lithosphere has to the strain, in the same way, the value of T_e that best fits at rigidity will be compute, as well as the

deflection that lithosphere experiments due to the load that support.

Flexural analysis

The case of a continental lithosphere which does not support any kind of load over its surface is illustrated in Figure 1a. The crust with density separate of the mantle with density by Mohorovicic layer, commonly known as Moho; now, when the same continental lithosphere is loaded with a mass as the topography, it shows that Moho suffers a downward deflection (figure 1b), the latest is associated with a value of flexural rigidity and a value of elastic thickness.

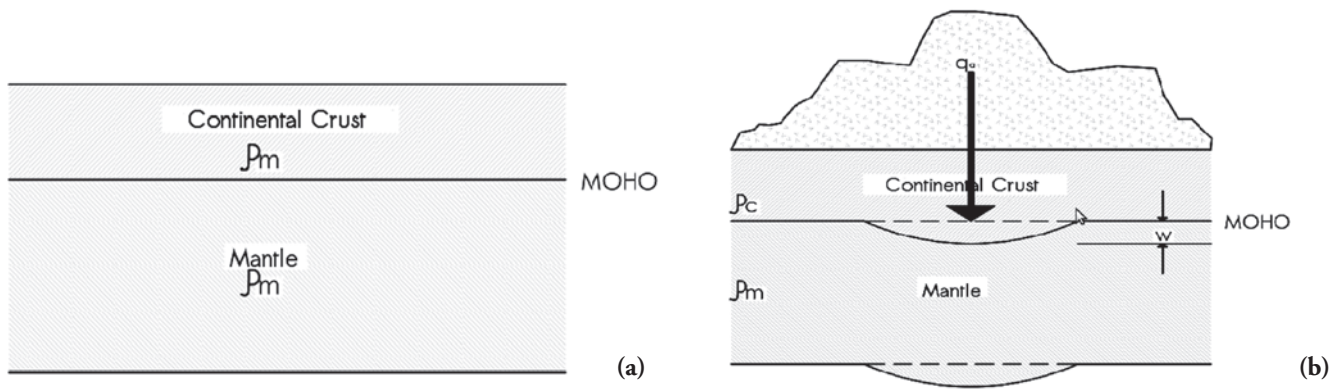


Figure 1. Behavior of Earth's Lithosphere. Modified from Turcotte (1982)

In flexural analysis must be assumed that continental lithosphere seems to a two-dimensional thin plate with an elastic behavior that rests over a viscous fluid as the mantle. Deflection that the plate holds up because topographic load differs in accordance with the variation of this over the surface. Flexure of an infinite elastic plate loaded with topography is described by the next expression.

$$D \frac{d^4 W}{dx^4} + \frac{d^2 W}{dx^2} + (\rho_m - \rho_c) g W(x) = g p_c h(x) \quad (1)$$

In equation (1), expression is the topographical load which is supported by an astenospherical restitution force and the flexural rigidity. Where moreover:

$$\rho_m = 3.3 \frac{gr}{cm^3} = \text{Mantle average density}$$

$$\rho_c = 2.8 \frac{gr}{cm^3} = \text{Crust average density}$$

$$g = 9.8 \frac{m}{s^2} = \text{Gravity acceleration}$$

$$h(x) = \text{Topographical Height}$$

$$x = \text{Distance along Profile}$$

In this way the flexural rigidity is given by equation (2), where elastic thickness T_e controls the flexural rigidity of all system. A numerical solution that employs finite difference technique, which approaches the derivatives that integrates the problem of ordinary differential equations where the solution is reduced until a lineal system, this allow computing a deflection profile which is the result of locate values of T_e across it.

$$D = \frac{ET_e^2}{12(1-\rho^2)} \quad (2)$$

Where:

$$E = 10Pa = \text{Young Modulus}$$

$$T_e = \text{Effective Elastic Thickness}$$

$$\rho = 0.25 = \text{Poisson Rate}$$

Bouguer anomaly that commonly has been associated with Moho geometry, it is the fundamental term to get the final values of elastic thickness, is obtained through a comparison between observed Bouguer anomaly in profile and Bouguer anomaly given by the model. So then, several values of T_e are introduced until obtaining the best fit between two quantities. When the final value of effective elastic thickness has been obtained, it is possible to find the value of flexural rigidity as well as a Moho deflection profile. Two kinds of models can be used to quantify the flexure of a plate subjected to a vertical load: Continuous plate model which describes a flexure of an infinite elastic plate due to a vertical load, and a broken plate model in which the load makes weight over a bound of the semi-infinite plate (Turcotte, 1982).

Methodological application

Flexural Analysis was executed over three (3) profiles, these profiles are showed in figure 2a, each one was computed to obtain simple Bouguer anomaly model from Free Air Anomaly map (figure 2b) calculated from Global Geopotential Models (for this study EIGEN-CG03C) and topographical heights. In this work, the continuous plate model was employed, and all computes of flexural analysis were made with open source software tAo (García, Fernández y Torné, 1997).

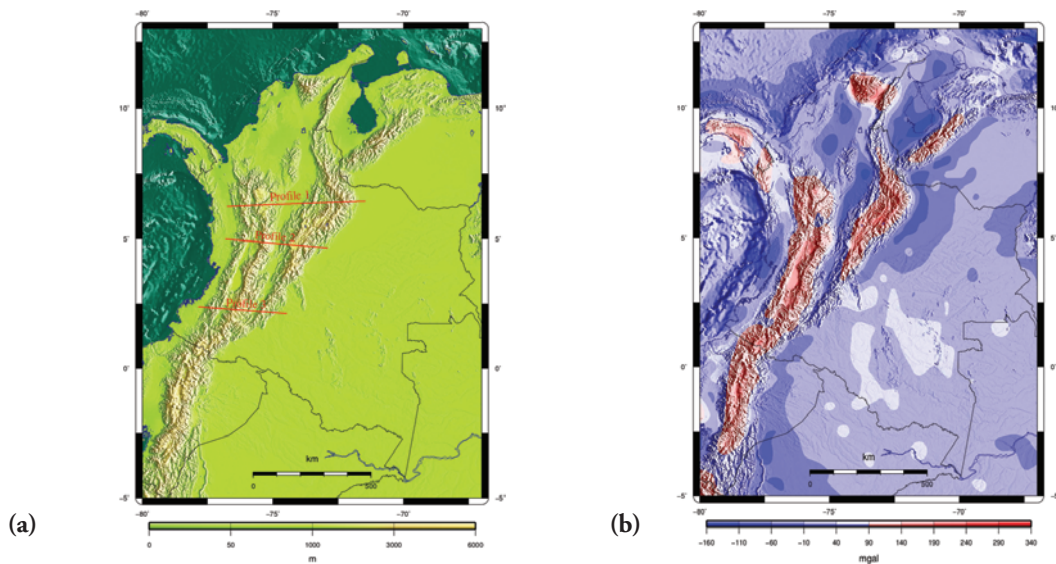


Figure 2. Profiles employed for flexural analysis and free air anomaly map calculated from EIGEN-CG03C

Profile 1 flexural analysis

This profile was drawn from coordinates, to ,; over a geographical area that covers mountain regions in Chocó, Antioquia, Boyacá and Santander. In whose geological formations the most important is Sierra Nevada del Cocuy with a height about at 5000 m.

In table 1 are showed the values associated to the deflection determined by the model, figure 3a shows the curve of flexure caused by the topographical load in this profile and

the figure 3b shows the fit established with the Bouguer anomaly curves that represents an elastic thickness of 12 km.

Table 1. Flexural analysis values for profile 1

Profile 1	
Dmax	5835.8 m
Mean Rigidity	$1.08e + 22$ Newton
Total Load Weight	$2.170e + 13$ N/m
Total Rest. Force	$2.164e + 13$ N/m

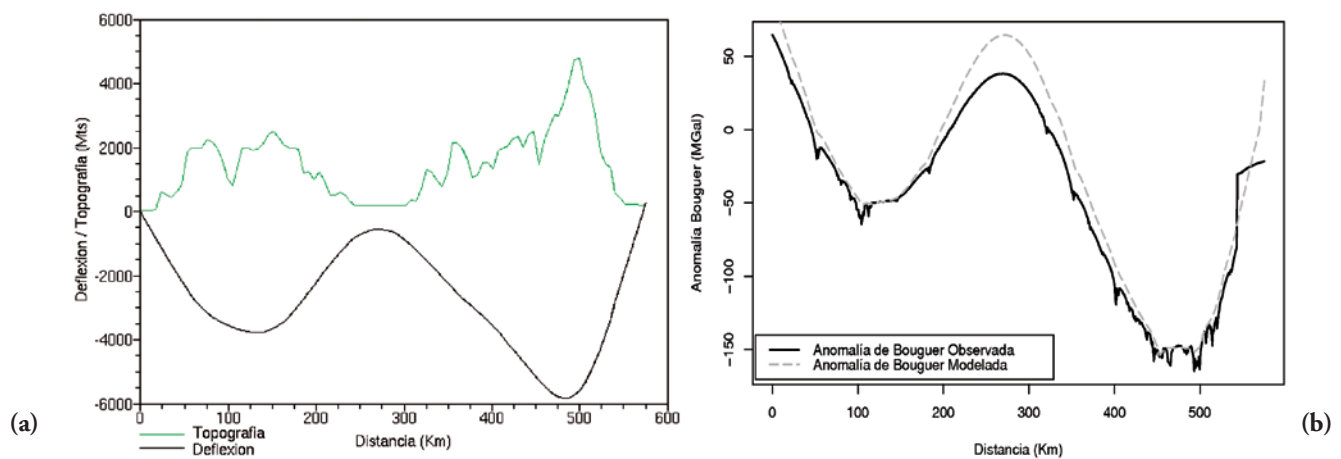


Figure 3. Profile curve deflection and Bouguer anomaly Fit for profile 1

Profile 2 flexural analysis

This section was drawn from coordinates, to, ; including a geographical area of mountain regions in Chocó, Huila, Tolima, Cundinamarca, among other Departments (States jurisdictions). In this profile, can be identified the area of the most important geological formations in Colombian Andes, the Nevados region.

In table 2 were entered the deflection associated values, the figure 4a shows the flexure curve drawn by the load, and figure 4b represents the fixed values of the Bouguer anomaly of the flexure model as well as the observed in

the gravity satellital model, that means an effective elastic thickness about 20 km.

Table 2. Flexural analysis values for profile 2

Profile 2	
Dmax	4561,1 m
Mean Rigidity	4,98e + 22 Newton
Total Load Weight	1,964e + 13 N/m
Total Rest. Force	1,971e + 13 N/m

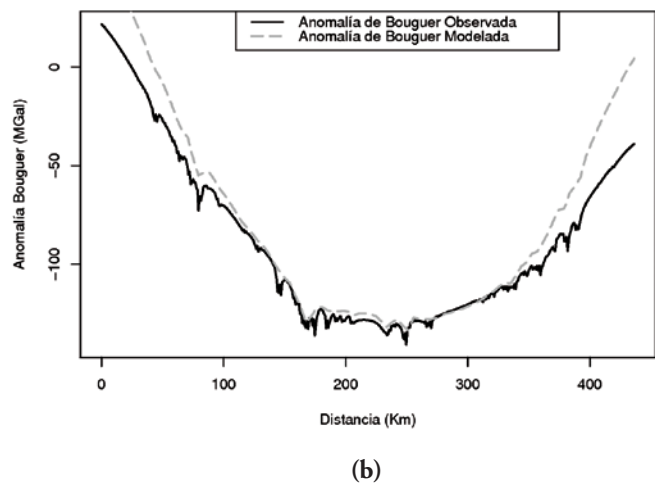
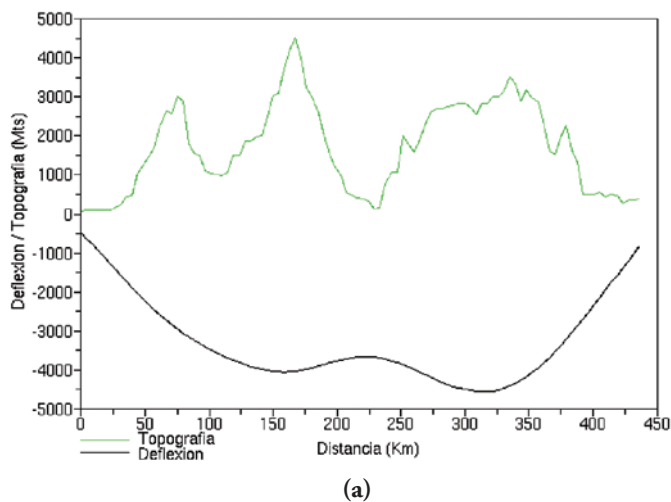


Figure 4. Profile curve deflection and Bouguer anomaly fit for profile 2

Profile 3 flexural analysis

The last profile used in this analysis crosses a geographical area from coordinates, to, he area includes mountain regions in Nariño, Huila and Caquetá. This profile contains the lowest heights of the study, due to that the area covers the origins of the Cauca and Magdalena valleys.

In table 3 are showed the parameters associated with deflection determined by the model, figure 5a shows the curve of flexure caused by the topographical load in this profile and the figure 5b shows the fit established with the Bouguer anomaly curves that represents an elastic thickness of 28 km.

Table 3. Flexural Analysis Values for Profile 3

Profile 3	
Dmax	4246,2 m
Mean Rigidity	1,37e+23 Newton
Total Load Weight	1,521e+13 N/m
Total Rest. Force	1,525e+13 N/m

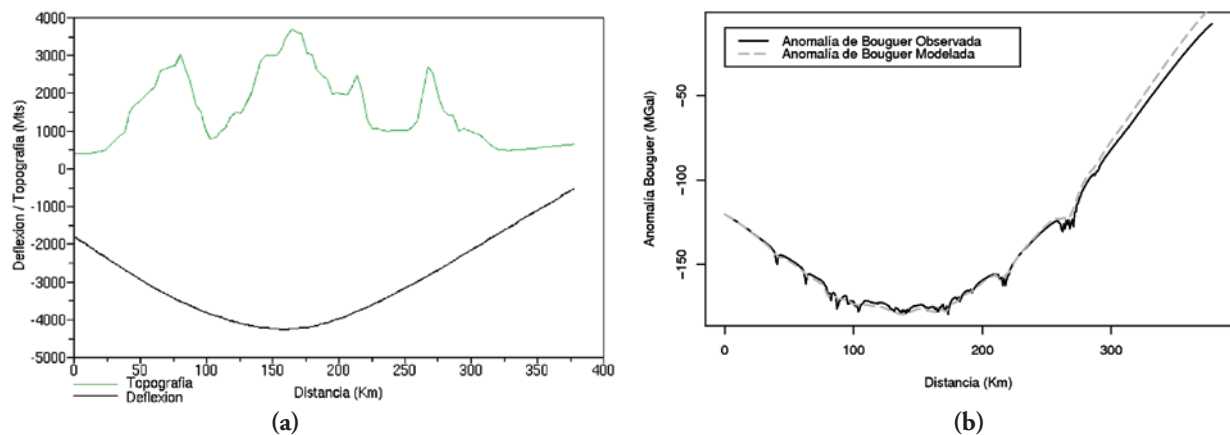


Figure 5. Profile curve deflection and Bouguer anomaly fit for profile 3

Discussion

The obtained results in this study can be analyzed from three parameters: flexural rigidity, Moho deflection and effective elastic thickness values. For the Colombian Andes (Kellogg, Salvador and Ojeda, 1995) shows an estimated mean value for flexural rigidity which is $1\text{E}+30$ Dina (approximately $1\text{E}+25$ Newton), but (Karner and Watts, 1983) whose research was developed over Mountain belts as Himalaya, Alpes and Apalachians obtaining values between $1\text{E}+25$ to $5\text{E}+25$ Newton; also is important knowing (Forsyth, 1985) got mean values between $1\text{E}+22$ to $5\text{E}+22$ Newton. These values compared with the obtained value in this work allow concluding that with the procedures here employed were obtained values that are in the expected limits. In concern with the Moho deflection (Ojeda, 2000) reports a maximum deflection value about 10 km for the eastern mountain belt, while in this work have been obtained maximum values of deflection in the order of 4 km to 6 km, which are directly related with effective elastic thickness values that presents a growing trend from north to south of the Country, but in this topic there are not studies that allow making a direct comparison, hence is difficult to conclude if obtained deflections are higher or are into the normal limits.

Conclusions

In this work was found a relation among growing trend of effective elastic thickness, flexural rigidity and mean rigidity from north to south of the Colombian Andes. Although this relation and the obtained values are not enough to determine what model represents distribution of strength of the continen-

tal lithosphere (Crème Brulle or Jelly Sandwich), the results are a light approximation to understand this phenomena.

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Acknowledgments

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